



Unified International
Mathematics Olympiad

UNIFIED INTERNATIONAL MATHEMATICS OLYMPIAD

CLASS - 09

Question Paper Code : 40109

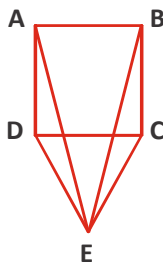
KEY

1	2	3	4	5	6	7	8	9	10
D	C	C	C	D	A	B	C	C	C
11	12	13	14	15	16	17	18	19	20
B	A	B	D	A	D	C	D	A	D
21	22	23	24	25	26	27	28	29	30
A	B	C	D	B	C	C	B	C	C
31	32	33	34	35	36	37	38	39	40
A,B,C	A,B,D	A,B,C,D	B,C,D	A,B,D	A	D	D	D	A
41	42	43	44	45	46	47	48	49	50
C	A	B	C	A	C	C	A	B	A

SOLUTIONS

MATHEMATICS - 1

01. (D) It is given that $\triangle CDE$ is an equilateral triangle



$$\angle CDE = \angle CED = \angle DEC = 60^\circ$$

It is also given that ABCD is a square

$$\angle ADC = \angle BCD = 90^\circ$$

$$\text{Now, } \angle ADE = \angle ADC + \angle CDE = 90^\circ + 60^\circ = 150^\circ \quad \dots (i)$$

$$\text{and } \angle BCE = \angle BCD + \angle DCE = 90^\circ + 60^\circ = 150^\circ \quad \dots (ii)$$

Thus, in \triangle s ADE and BCE, we have

$$AD = BC \text{ [Sides of same square]}$$

$$DE = CD \text{ [Sides of an equilateral triangle]}$$

$$\text{and } \angle ADE = \angle BCE \text{ [from (i)]}$$

So, by using SAS congruence criterion, we obtain

$$\triangle ADE \cong \triangle BCE$$

$$\angle ADE = 90^\circ + 60^\circ = 150^\circ$$

In $\triangle ADE$, $AD = DE$

$$\therefore x + x + 150^\circ = 180^\circ$$

$$2x = 30^\circ$$

$$x = \frac{30^\circ}{2} = 15^\circ$$

$$\therefore \angle BEC = 15^\circ$$

But $\angle DEC = 60^\circ$

$$x + \angle AEB + x = 60^\circ$$

$$15^\circ + \angle AEB + 15^\circ = 60^\circ$$

$$\angle AEB = 60^\circ - 30^\circ$$

$$\angle AEB = 30^\circ$$

02. (C) $x = \frac{9}{4}$

$$\frac{1}{\sqrt{6} + \sqrt{5} - \sqrt{11}} = \frac{1}{(\sqrt{6} + \sqrt{5}) - \sqrt{11}}$$

$$\times \frac{(\sqrt{6} + \sqrt{5}) + \sqrt{11}}{(\sqrt{6} + \sqrt{5}) + \sqrt{11}}$$

$$= \frac{(\sqrt{6} + \sqrt{5} + \sqrt{11})}{(\sqrt{6} + \sqrt{5})^2 - (\sqrt{11})^2}$$

$$= \frac{(\sqrt{6} + \sqrt{5} + \sqrt{11})}{6 + 5 + 2\sqrt{6} \times \sqrt{5} - 11}$$

$$= \frac{(\sqrt{6} + \sqrt{5} + \sqrt{11})}{2\sqrt{30}} \times \frac{(\sqrt{30})}{\sqrt{30}}$$

$$= \frac{\sqrt{6} \times \sqrt{30} + \sqrt{5} \times \sqrt{30} + \sqrt{11} \times \sqrt{30}}{2 \times 30}$$

$$= \frac{6\sqrt{5} + 5\sqrt{6} + \sqrt{330}}{60}$$

03. (C) Given the sides ratio = 3 : 4 : 5 = 3x : 4x : 5x

$$\therefore a = 3x, b = 4x \text{ \& } c = 5x$$

Given $a + b + c = 156 \text{ m}$

$$3x + 4x + 5x = 156 \text{ m}$$

$$12x = 156 \text{ m}$$

$$x = \frac{156}{12} = 13 \text{ m}$$

$$\therefore a = 3x = 3 \times 13 \text{ m} = 39 \text{ m}$$

$$b = 4x = 4 \times 13 \text{ m} = 52 \text{ m}$$

$$c = 5x = 5 \times 13 \text{ m} = 65 \text{ m}$$

$$c^2 = a^2 + b^2$$

\therefore a, b, c are the sides of a right angled triangle

\therefore Area

$$= \frac{1}{2} \times ab = \frac{1}{2} \times 39 \times 52 \text{ m}^2 = 1014 \text{ cm}^2$$

04. (C)

$3x - 4$	$12x^3 + 76x^2 + 155x + 100$	$4x^2 + 20x + 25$
	$12x^3 + 16x^2$	
	$(-)$ $(-)$	
	$60x^2 + 155x$	
	$60x^2 + 80x$	
	$(-)$ $(-)$	
	$75x + 100$	
	$75x + 100$	
	$(-)$ $(-)$	
	0	

$$\therefore \sqrt{\frac{12x^3 + 76x^2 + 155x + 100}{3x + 4}}$$

$$= \sqrt{4x^2 + 20x + 25}$$

$$= \sqrt{(2x)^2 + 2(2x)(5) + 5^2}$$

$$= \sqrt{(2x + 5)^2} = (2x + 5)$$

$$05. (D) \quad \frac{1}{3-\sqrt{8}} = \frac{1}{3-\sqrt{8}} \times \frac{3+\sqrt{8}}{3+\sqrt{8}} = \frac{3+\sqrt{8}}{3^2-(\sqrt{8})^2}$$

$$= \frac{3+\sqrt{8}}{9-8} = 3+\sqrt{8}$$

$$\frac{1}{\sqrt{8}-\sqrt{7}} = \frac{1}{\sqrt{8}-\sqrt{7}} \times \frac{\sqrt{8}+\sqrt{7}}{\sqrt{8}+\sqrt{7}}$$

$$= \frac{\sqrt{8}+\sqrt{7}}{(\sqrt{8})^2-(\sqrt{7})^2} = (\sqrt{8}+\sqrt{7})$$

$$\therefore \text{LHS} = (3+\sqrt{8}) - (\sqrt{8}+\sqrt{7}) + (\sqrt{7}+\sqrt{6})$$

$$- (\sqrt{6}+\sqrt{5}) + (\sqrt{5}+2)$$

$$= 3 + \sqrt{8} - \sqrt{8} - \sqrt{7} + \sqrt{7} + \sqrt{6} - \sqrt{6}$$

$$- \sqrt{5} + \sqrt{5} + 2 = 5$$

06. (A) Given diagonal of a cube = diameter of a sphere

$$\therefore \sqrt{3}a = 2 \text{ cm}$$

$$\therefore a = \frac{2\text{cm}}{\sqrt{3}}$$

$$\text{Volume of cube} = a^3 = \left(\frac{2}{\sqrt{3}}\text{cm}\right)^3$$

$$= \frac{8}{3\sqrt{3}}\text{cm}^3$$

$$07. (B) \quad s = \frac{91 \text{ cm} + 80 \text{ cm} + 109 \text{ cm}}{2}$$

$$= \frac{280 \text{ cm}}{2}$$

$$= 140 \text{ cm}$$

$$\text{Area of } D = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{140 \text{ cm} \times 49 \text{ cm} \times 60 \text{ cm} \times 31 \text{ cm}}$$

$$= \sqrt{12759600} \text{ cm}^2$$

3	12759600	3572.0
9		
65	375	
707	325	
7142	5096	
71420	4949	
	14500	
	14284	
	31600	
	0	
	31600	

$$= 3,572 \text{ cm}^2$$

$$\text{But } \frac{1}{2} \times h \times 109 \text{ cm} = 3,572 \text{ cm}^2$$

$$\therefore h = \frac{3,572 \text{ cm}^2 \times 2}{109 \text{ cm}}$$

$$h = 65.54 \text{ cm}$$

$$08. (C) \quad \frac{(32)^{0.2} + (81)^{0.25}}{(256)^{0.5} - (121)^{0.5}} = \frac{(2^3)^{1/5} + (3^4)^{1/4}}{(2^8)^{1/2} - (11^2)^{1/2}}$$

$$= \frac{2^{5 \times \frac{1}{5}} + 3^{4 \times \frac{1}{4}}}{2^{8 \times \frac{1}{2}} - 11^{2 \times \frac{1}{2}}} = \frac{2+3}{2^4-11} = \frac{5}{16-11}$$

$$= \frac{5}{5} = 1$$

$$09. (C) \quad \angle \text{TSR} = 80^\circ$$

$$\angle \text{OST} = \angle \text{OST} = \frac{180^\circ - 50^\circ}{2} = 65^\circ$$

$$x^\circ = 80^\circ - 65^\circ = 15^\circ$$

$$10. (C) \quad \angle \text{BAD} = \frac{1}{2} \angle \text{BOD}$$

$$= \frac{1}{2} \times 140^\circ = 70^\circ$$

$\angle \text{DCP} = \angle \text{BAD}$ [Since exterior angle of a cyclic quadrilateral is equal to the interior opp. angle.]

$$\therefore \angle \text{DCP} = \angle \text{BAD} = 70^\circ$$

11. (B) Given $\angle A = \angle B + \angle C$ In $\triangle ABC$

But $\angle A + \angle B + \angle C = 180^\circ$

$$\Rightarrow \angle A + \angle A = 180^\circ$$

$$[\therefore \angle B + \angle C = \angle A]$$

$$\angle A = 90^\circ$$

12. (A) Gives P lies $x = -5$ line & $y = 1$ line

$$\therefore P = (-5, 1)$$

13. (B) $x^2 - z^2 + y^2 - p^2 + 2pz - 2xy$

$$= (x - y)^2 - (p - z)^2$$

$$= (x - y + p - z)(x - y - p + z)$$

14. (D) Let 'k' to be added to $(x^{46} - 3x^{35} + 2x^{24} + 5)$

So, that it is exactly divisible by $(x + 1)$

$$\therefore p(x) = x^{46} - 3x^{35} + 2x^{24} + 5 + k \text{ and } p(-1) = 0$$

$$p(-1) = (-1)^{46} - 3(-1)^{35} + 2(-1)^{24} + 5 + k = 0$$

$$1 - 3(-1) + 2 + 5 + k = 0$$

$$1 + 3 + 7 + k = 0$$

$$k = -11$$

15. (A) Given $2x + 1^\circ + 4x - 10^\circ + x + 15^\circ + x + 10^\circ = 360^\circ$

$$8x + 16^\circ = 360^\circ$$

$$8x = 344^\circ$$

$$x = 43^\circ$$

16. (D) $S = \pi r l = \pi r \sqrt{r^2 + h^2}$

$$V = \frac{1}{3} \pi r^2 h$$

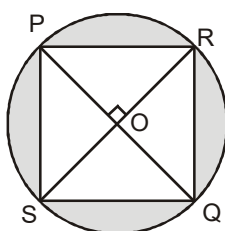
$$\therefore 3\pi Vh^3 + 9V^2 - S^2h^2 = 3\pi \times \frac{1}{3} \pi r^2 h \times h^3 +$$

$$9 \times \frac{1}{9} \pi^2 r^4 h^2 - \pi^2 r^2 (r^2 + h^2) h^2$$

$$= \pi^2 r^2 h^4 + \pi^2 r^4 h^2 - \pi^2 r^4 h^2 - \pi^2 r^2 h^4$$

$$= 0$$

17. (C) Let the diagonals meet at O as shown in the figure



$$\angle POS = \angle ROQ = 90^\circ$$

Also $OP = OQ = OS = OR$, i.e., the diagonals are equal and bisect at right angles. Clearly, PRQS is a square

18. (D) $\angle y + \angle G = 180^\circ$
....(Linear pair axiom)

$$\text{or } \angle y + \angle 125^\circ = 180^\circ$$

$$\therefore \angle y = 180^\circ - 125^\circ = 55^\circ$$

AB || DE and BD cuts them

$$\therefore \angle D = \angle B \quad \dots(\text{Alt. } \angle \text{s})$$

$$\text{or } \angle D = 65^\circ \quad \dots(\text{i})$$

Again BD || FG and DF cuts them

$$\therefore \angle F = \angle D \quad \dots(\text{Alt. } \angle \text{s})$$

$$= 65^\circ \quad \text{Using (i) } \dots(\text{ii})$$

In $\triangle EFG$, EG is produced

$$\therefore \angle x + \angle F = \angle G = 125^\circ$$

$$\therefore \angle x + 65^\circ = 125^\circ \text{ [Using (ii)]}$$

$$\text{or } \angle x = 125^\circ - 65^\circ = 60^\circ$$

Hence $\angle x = 60^\circ$ and $\angle x = 55^\circ$

$$\angle x - \angle y = 60^\circ - 55^\circ = 5^\circ$$

19. (A) Given in $\triangle ABC$, $AB = AC \Rightarrow \angle C = \angle B = 35^\circ$

In $\triangle ABD$ and $\triangle ACD$

$$\overline{AB} = \overline{AC} \quad (\because \text{side \& given})$$

$$\overline{BD} = \overline{DC} \quad (\because \text{side \& given})$$

$$\overline{AD} = \overline{AD} \quad (\because \text{side \& common})$$

$$\therefore \triangle ABD \cong \triangle ACD \quad [\because \text{SSS congruency}]$$

$$\therefore \angle BDA = \angle CDA \quad [\because \text{CPCT}]$$

But $\angle BDA + \angle CDA = 180^\circ$

$$\angle BDA + \angle BDA = 180^\circ$$

$$2\angle BDA = 180^\circ$$

$$\angle BDA = \frac{180^\circ}{2} = 90^\circ$$

In $\triangle BAD$, $35^\circ + 90^\circ + \angle BAD = 180^\circ$

$$125^\circ + \angle BAD = 180^\circ$$

$$\angle BAD = 180^\circ - 125^\circ$$

$$\angle BAD = 55^\circ$$

20. (D) $a + b - c = a + b - c + c - c$
 $= a + b + c - 2c$
 $= 2s - 2c$
 $= 2(s - c)$
 Similarly $(a - b + c) = 2(s - b)$
 $(b + c - a) = 2(c - a)$
 $\therefore (a + b + c)(a + b - c)(a - b + c)$
 $(b + c - a) = 2s \times 2(s - a) \times 2(s - b) \times 2(s - c)$
 $= 16 \cdot 3(s - a)(s - b)(s - c)$
 $= 16(\sqrt{s(s - a)(s - b)(s - c)})^2$
 $= 16\Delta^2$

21. (A) Given $h = r$
 Volumes ratio of cone, hemisphere and cylinder = $\frac{1}{3}\pi r^2 h : \frac{2}{3}\pi r^3 : \pi r^2 h$
 $= \frac{1}{3}\pi r^2(r) : \frac{2}{3}\pi r^3 : \pi r^2(r)$
 $= \frac{\pi r^3}{3} : \frac{2}{3}\pi r^3 : \pi r^3$
 $= \frac{1}{3} \times 3 : \frac{2}{3} \times 3 : 1 \times 3$
 $= 1 : 2 : 3$

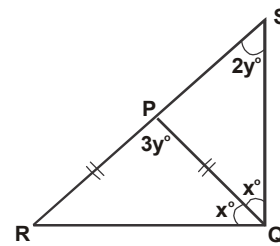
22. (B) In $\triangle ABC$, $40^\circ + 90^\circ + \angle B = 180^\circ$
 $\angle B = 180^\circ - 130^\circ = 50^\circ$
 In $\triangle BDE$, $\angle B + \angle D + \angle BED = 180^\circ$
 $50^\circ + x + 100^\circ = 180^\circ$
 $x = 180^\circ - 150^\circ$
 $x = 30^\circ$

23. (C) Long division method: In this method, we first divide $x^3 + 13x^2 + 32x + 20$ by $(x + 2)$ to obtain the quotient as a quadratic in x and then we factorize the quotient by the methods discussed earlier.

$$\begin{array}{r} x+2 \overline{) x^3 + 13x^2 + 32x + 20} \\ \underline{x^3 + 2x^2} \\ 11x^2 + 32x \\ \underline{11x^2 + 22x} \\ 10x + 20 \\ \underline{10x + 20} \\ 0 \end{array}$$

$x^3 + 13x^2 + 32x + 20 = (x + 2)(x + 1)(x + 10)$
 $(x + 10) = (x + 2)(x^2 + 11x + 10)$
 $= (x + 2)(x^2 + x + 10x + 10) = (x + 2)\{(x^2 + x) + (10x + 10)\}$
 $= (x + 2)\{x(x + 1) + 10(x + 1)\} = (x + 2)(x + 1)(x + 10)$
 Hence, $x^3 + 13x^2 + 32x + 20 = (x + 2)(x + 1)(x + 10)$

24. (D) Given, $PR = PQ = \angle PRQ = \angle RPQ = x^\circ$



$\Rightarrow x^\circ + x^\circ + 3y^\circ = 180^\circ$
 $\Rightarrow 2x + 3y = 180^\circ$ (i)
 and $3y^\circ = 2y^\circ + x^\circ$
 $\Rightarrow x^\circ = y^\circ$ (ii)

From (i) and (ii) we get
 $x^\circ = y^\circ = 36^\circ$

$\therefore \angle RPQ = 3y^\circ = 3 \times 36^\circ = 108^\circ$

25. (B) Sum of the shaded angles = $5 \times$ sum of the angles of a triangle

$\frac{\text{Complete angle}}{2}$
 $= 5 \times 180^\circ - \frac{360^\circ}{2}$
 $= 900^\circ - 180^\circ$
 $= 720^\circ$

26. (C) Given $x - \frac{1}{x} = (3 + 2\sqrt{2})$

Cubing on both sides

$$x^3 - \frac{1}{x^3} - 3 \cancel{x} \times \frac{1}{\cancel{x}} (x - \frac{1}{x}) = (3 + 2\sqrt{2})^3$$

$$x^3 - \frac{1}{x^3} - 3(3 + 2\sqrt{2}) = 3^3 + 3 \times 3^2(2\sqrt{2}) + 3 \times 3(2\sqrt{2})^2 + (2\sqrt{2})^3$$

$$x^3 - \frac{1}{x^3} - 9 - 6\sqrt{2} = 27 + 54\sqrt{2} + 72 + 16\sqrt{2}$$

$$x^3 - \frac{1}{x^3} - 99 + 70\sqrt{2} + 9 + 6\sqrt{2}$$

$$= 108 + 76\sqrt{2}$$

27. (C) Length of each edge of the cube = 44 cm

$$\text{Volume of the cube} = (44 \times 44 \times 44) \text{ cm}^3$$

Radius of each bullet, $r = 2$ cm

$$\text{Volume of each bullet} = \left(\frac{4}{3}\pi r^3\right) \text{ cm}^3$$

$$= \left(\frac{4}{3} \times \frac{22}{7} \times 2 \times 2 \times 2\right) \text{ cm}^3 = \frac{704}{21} \text{ cm}^3$$

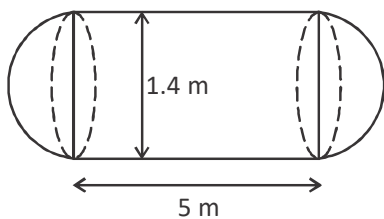
Number of bullets formed =

$$\frac{\text{volume of the cube in cm}^3}{\text{Volume of each bullet in cm}^3}$$

$$= \left(44 \times 44 \times 44 \times \frac{21}{704}\right) = 2541$$

Hence, the number of bullets formed is 2541

28. (B) We have, Diameter of the cylinder = 1.4 m



$$r = \text{Radius of the cylinder} = \frac{1.4\text{m}}{2} = 0.7\text{m}$$

and $h = \text{Length of the cylinder} = 5$ m

$$\therefore S_1 = \text{Surface area of the cylinder} = 2\pi rh$$

Clearly, Radius of the hemisphere = r .

$$\therefore S_2 = \text{Surface area of two hemi-spheres} = 2 \times 2\pi r^2 = 4\pi r^2$$

Let S be the total surface area of storage tank. Then,

$$S = S_1 + S_2 = 2\pi rh + 4\pi r^2 = 2\pi r(h + 2r)$$

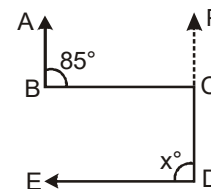
$$S = 2 \times \frac{22}{7} \times 0.7(5 + 2 \times 0.7)$$

$$= 2 \times 22 \times 0.1 \times 6.4 = 28.16 \text{ m}^2$$

Rate of painting = Rs. 10 per square metre.

$$\therefore \text{Cost of painting} = \text{Rs.}(10 \times 28.16) = \text{Rs. } 281.60$$

29. (C) Extend the line DC to a point P, such that $AB \parallel CP$,



Then $\angle BCP = \angle EDC = x^\circ$
(Corresponding angles)

$$\text{Also, } \angle ABC + \angle BCP = 180^\circ$$

$$\Rightarrow \angle BCP = 95^\circ$$

$$\text{and } \angle BCP = \angle EDC = 95^\circ$$

30. (C) $\angle ACD = \angle BAC + \angle B = 30^\circ + 40^\circ = 70^\circ$

$$x = \angle ACD + 50^\circ = 70^\circ + 50^\circ$$

$$x = 120^\circ$$

MATHEMATICS - 2

31. (A, B, C)

$$\angle BCD = 36^\circ + 30^\circ = 66^\circ$$

$$\therefore \angle B = \angle BCD$$

$$AB \parallel CD \quad \dots\dots (1)$$

$$\angle E + \angle ECD = 150^\circ + 30^\circ = 180^\circ$$

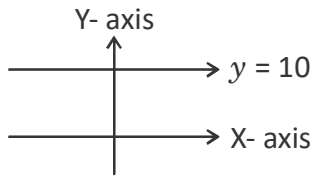
$$\therefore EF \parallel CD \quad \dots\dots (2)$$

From equation (1) and (2) $AB \parallel EF$

32. (A, B, D)

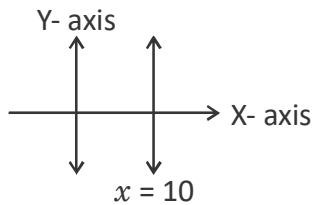
(0, 0) has on $x = y$ line.

∴ option 'A' is true



$y = 10$ line is perpendicular to y -axis

∴ option 'B' is true



$x = 10$ line is parallel to y -axis

∴ Option 'D' is correct

33. (A, B, C, D)

$$= \frac{1}{3} \pi r^2 h = 9856 \text{ cm}^3$$

$$= \frac{1}{3} \times \frac{22}{7} \times 14^2 \times 14 \times h \text{ cm}^3 = 9856 \text{ cm}^3$$

$$h = \frac{9856 \times 3 \times \frac{7}{22} \times \frac{7}{22} \times \frac{1}{14}}{1} \text{ cm}^3$$

$$h = 48 \text{ cm}$$

$$l^2 = h^2 + r^2 = 48^2 + 14^2$$

$$= \sqrt{2304 + 196}$$

$$l = \sqrt{2500}$$

$$l = 50 \text{ cm}$$

$$\text{CSA of a cone} = \pi r l$$

$$= \frac{22}{7} \times 14^2 \text{ cm} \times 50 \text{ cm}$$

$$= 2200 \text{ cm}^2$$

$$\text{TSA of a cone} = \pi r l + \pi r^2$$

$$= 2200 \text{ cm}^2 + \frac{22}{7} \times 14^2 \text{ cm} \times 14 \text{ cm}$$

$$= 2200 \text{ cm}^2 + 616 \text{ cm}^2$$

$$= 2816 \text{ cm}^2$$

34. (B, C, D)

$$(x^2 - 4x)(x^2 - 4x - 1) - 20$$

$$= (x^2 - 4x)^2 - (x^2 - 4x) - 20$$

$$= y^2 - y - 20, \text{ where } y = x^2 - 4x$$

$$= y^2 - 5y + 4y - 20$$

$$= (y^2 - 5y) + (4y - 20)$$

$$= y(y - 5) + 4(y - 5)$$

$$= (y - 5)(y + 4)$$

$$= (x^2 - 4x - 5)(x^2 - 4x + 4)$$

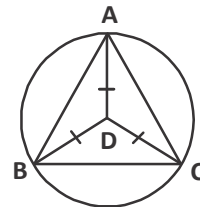
[Replacing y by $x^2 - 4x$]

$$= (x^2 - 5x + x - 5)(x^2 - 2 \times x \times 2 + 2^2)$$

$$= \{x(x - 5) + (x - 5)\}(x - 2)^2 = (x - 5)(x + 1)(x - 2)^2$$

35. (A, B, D)

'D' is equidistant from A, B, and C.



∴ 'D' is a circumcentre

$$\therefore \angle BAC = \frac{1}{2} \angle BDC = \frac{1}{2} \times 100^\circ$$

$$\angle BAC = 50^\circ$$

$$\angle BCA = \frac{1}{2} \angle BDA = \frac{1}{2} \times 144^\circ$$

$$\angle BCA = 72^\circ$$

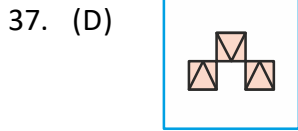
$$\angle ABC = \frac{1}{2} \angle ADC = \frac{1}{2} \times 116^\circ = 58^\circ$$

$$\angle ABC = 58^\circ$$

REASONING

36. (A) $\frac{QRST}{2} \quad \frac{UVWXYZ}{5} \quad \frac{ABCDEFGH}{7} \quad \frac{IJKLMNOPQRS}{10}$

Number of letters skipped between adjacent letters in the series is in the order of 2, 5, 7, 10.



38. (D) Initially number of lines are equal to the number of dark triangles and then white triangle is equal to the number of lines.

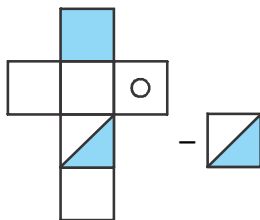


39. (D) $\left. \begin{array}{l} 3 \times 3 = 9 \\ 4 \times 4 = 16 \end{array} \right\} 916$

$\left. \begin{array}{l} 2 \times 2 = 4 \\ 6 \times 6 = 36 \end{array} \right\} 436$

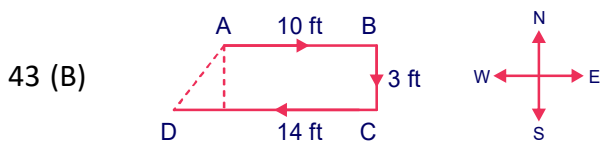
$\left. \begin{array}{l} 1 \times 1 = 1 \\ 5 \times 5 = 25 \end{array} \right\} 125$

40. (A) Only one cube has only one face painted red.



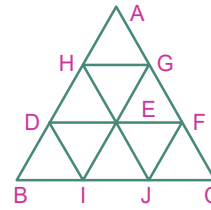
41. (C)

42. (A) $4 \xrightarrow{+1^2} 5 \xrightarrow{+2^2} 9 \xrightarrow{+3^2} 18 \xrightarrow{+4^2} 34 \xrightarrow{+5^2} 59$



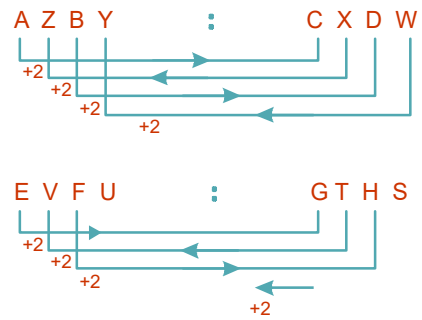
Required distance $AD = \sqrt{3^2 + (14 - 10)^2}$
 $= \sqrt{9 + 16}$
 $= 5 \text{ ft}$

44. (C) There are 15 parallelograms in the given figure.

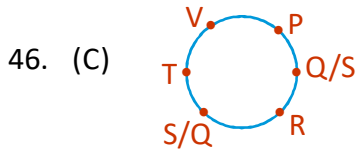


- | | |
|----------|----------|
| 1. BDEI | 2. EFJI |
| 3. DEJI | 4. EFCJ |
| 5. DEGH | 6. EFGH |
| 7. EGAH | 8. BHGI |
| 9. GHJC | 10. AGID |
| 11. AFJH | 12. DHEI |
| 13. EGFI | 14. DFJB |
| 15. DFCI | |

45. (A)



CRITICAL THINKING



47. (C) House 17 is 6th from the right side. Now on the opposite lane houses start from number 23. 6th house from the right side on opposite lane would be 28th

44	43	42	41	40	39	38	37	36	35	34	33	32	31	30	29	28	27	26	25	24	23
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22

48. (A) In fig. (X), one of the dots lies in the region common to the square and the triangle only, another dot lies in the region common to the circle and the triangle only and the third dot lies in the region common to the triangle and the rectangle only. In fig. (2), there is no region common to the square and the triangle only. In fig. (3), there is no region common to the circle and the triangle only. In fig. (4) there is no region common to the triangle and the rectangle only. Only fig. (1) consists of all the three types of regions.

49. (B) The statement talks of Jade plants only and not “all plants with thick leaves”. So, I does not follow. Also, since Jade plants require little water, so they can be grown in places where water is not in abundance so, II follows.

50. (A) Because Mr. Sachin spends many hours during the weekend working in his vegetable garden, it is reasonable to suggest that he enjoys this work. There is no information to suggest that he does not like classical music. Although Mrs. Sanchez likes to cook, there is nothing that indicates she cooks vegetables (choice c). Mrs. Sachin likes to read, but there is no information regarding the types of books she reads (choice d).

The End
